

3. e)  $k(x) = -f(-x)$  → you reflect the parent graph twice: once on  $x$  axis and once on  $y$  axis.

$$D = \{x \in \mathbb{R}, -6 \leq x \leq 2\}$$

$$R = \{y \in \mathbb{R}, -3 \leq y \leq -1\}$$

4. d)  $f(x) = \frac{1}{x-3} - 6$       $g(x) = -f(-x)$

$$g(x) = -\left(\frac{1}{-x-3} - 6\right)$$

$$= -\left(\frac{-1}{x+3} - 6\right) = \frac{1}{x+3} + 6$$

e)  $f(x) = -\sqrt{x-2} + 5$       $g(x) = f(-x)$

$$g(x) = -\sqrt{-x-2} + 5$$

f)  $f(x) = \sqrt{x+9} - 1$       $g(x)$

$$4 f) \quad f(x) = \sqrt{x+9} - 1 \quad g(x) = -f(-x)$$

$$g(x) = -(\sqrt{-x+9} - 1)$$

$$g(x) = -\sqrt{-x+9} + 1$$

5. a)  $g(x)$  is reflection of  $f(x)$  on  $y$  axis,  $= f(-x)$

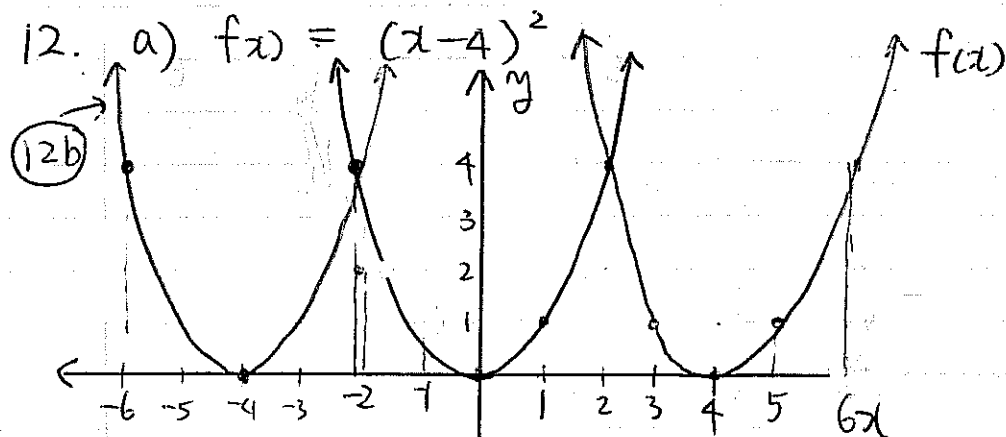
b)  $g(x)$  is reflection of  $f(x)$  on  $x$  axis,  $= -f(x)$

c)  $g(x)$  is " " " "  $x$  axis and  $y$  axis so  $\Rightarrow -f(-x)$

6. reflected on both  $y$  axis and  $x$  axis.

7. ① Reflection on  $x$  axis (generally speaking)  $\rightarrow$  Domain is not changed but range is changed.

② Reflection on  $y$  axis (generally speaking)  $\rightarrow$  Domain is changed, but range is not changed.



#12 c)  $h(x) = (x+4)^2$  or translate  $f(x)$  to the left 8 units.

$$b) g(x) = f(-x) = (-x-4)^2$$

$$\therefore g(x) = (-x-4)^2$$

$$d) g(x) = (-x-4)^2$$

$$= [-1(x+4)]^2 = (-1)^2 \cdot (x+4)^2$$

$$g(x) = (x+4)^2 = h(x)$$

e) reflection in the  $x$  axis  $\rightarrow -f(x) = -(x-4)^2$

$$I(x) = -(x-4)^2$$

$$J(x) = -(x+4)^2 \text{ (no translation has occurred)}$$

Answer: NO reflection in the  $x$  axis just changes the orientation. (not position)

f) Yes it works as long as the graph is symmetrical about a vertical line.

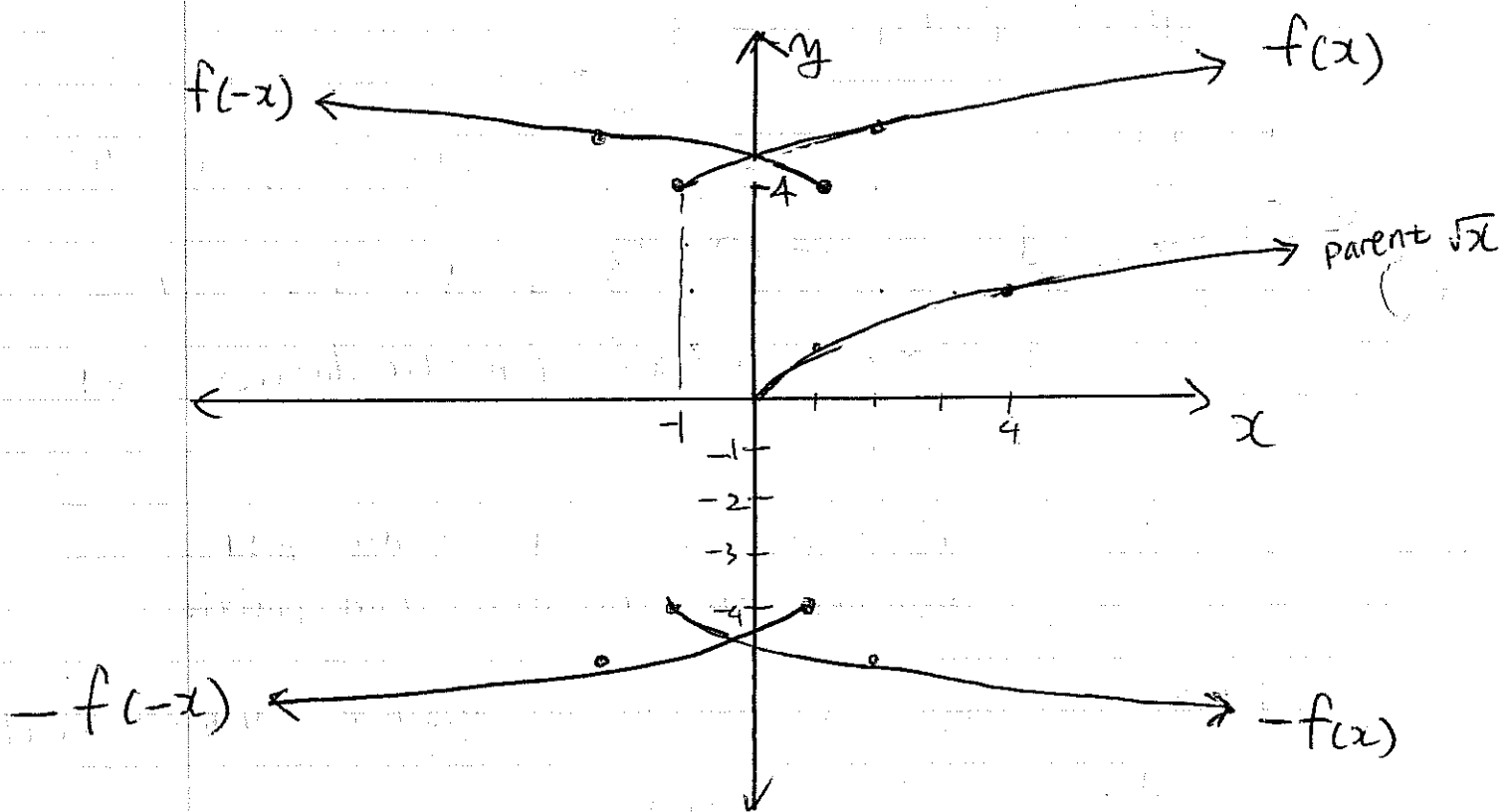
#13a) Base Function =  $f(x) = \sqrt{x}$  arrow without gravity

shift up by 3 and left by 2.

$$\begin{aligned} \#13b) \quad -f(x) &= -(\sqrt{x+2} + 3) \\ &= -\sqrt{x+2} - 3 \end{aligned}$$

$$\begin{aligned} -f(-x) &= -(\sqrt{-x+2} + 3) \\ &= -\sqrt{-x+2} - 3 \end{aligned}$$

$$f(-x) = \sqrt{-x+2} + 3$$



$$f(x) \rightarrow D = \{x \in \mathbb{R}, x \geq -1\} \quad R = \{y \in \mathbb{R}, y \geq 4\}$$

$$f(-x) \rightarrow D = \{x \in \mathbb{R}, x \leq 1\} \quad R = \{y \in \mathbb{R}, y \geq 4\}$$

$$-f(x) \rightarrow D = \{x \in \mathbb{R}, x \geq -1\} \quad R = \{y \in \mathbb{R}, y \leq -4\}$$

$$-f(-x) \rightarrow D = \{x \in \mathbb{R}, x \leq 1\} \quad R = \{y \in \mathbb{R}, y \leq -4\}$$