

Extra Factoring Practice

Feb 12

MPM2D

$$1) \quad 6m^3 - 10m^2t + 6mt^2$$

\swarrow \searrow
 $2m$

$$= 2m(3m^2 - 5mt + 3t^2) \quad \text{HT: } ax^2 + bx + c$$

$$a = 3 \quad b = -5t \quad c = 3t^2$$

$$ac = 3 \times 3t^2 = 9t^2 \quad b = -5t$$



$$= 2m(3m^2 - 5mt + 3t^2)$$

$$2) \quad x^6 - x^5 + x^4 - x^3 + x^2$$



$$= x^2(x^4 - x^3 + x^2 - x + 1)$$

$$3) \quad 5m(2m+1) - 4(2m+1)$$

$$= (2m+1)(5m-4)$$

$$4) \quad x^3 - x^2y + xy^2 - y^3$$

$$= x^2(x-y) + y^2(x-y)$$

$$= (x^2 + y^2)(x-y)$$

$$5) x^2 + 7x + 10 \quad a=1, c=10, b=7$$
$$ac = 1 \times 10 = 10 \rightarrow 5 \times 2$$
$$= (x+5)(x+2)$$

$$6) w^2 - 13w + 42 \quad a=1, c=42, b=-13$$
$$ac = 42 \rightarrow (-6) \times (-7)$$

$$7) 3g^2 - 6g - 45 \quad a=1, b=-2, c=-15$$
$$= 3(g^2 - 2g - 15) \quad ac = -15 \rightarrow (-5) \times 3$$
$$= 3(g-5)(g+3)$$

$$8) x^2 + xy - 12y^2 \xrightarrow{\text{HT}} a=1, b=y, c=-12y^2$$
$$= (x+4y)(x-3y) \quad (4y) \times (-3y)$$

$$9) 6x^2 - 7x - 20 \quad \text{HT} \quad a=6, b=-7, c=-20$$
$$ac = 6 \times -20 = -120$$
$$= 6x^2 + 8x - 15x - 20$$
$$= +4) - 15(x-4) \quad (8) \times (-15) \quad \checkmark$$

$$10) 6m^2 - 7m - 3 \quad \text{HT} \quad a=6, b=-7, c=-3$$
$$ac = 6 \times -3 = -18$$
$$= 6m^2 - 9m + 2m - 3 \quad b = -7 \quad (-9) \times 2$$
$$= 2m(3m+1) - 3(3m+1)$$
$$= (3m+1)(2m-3)$$

Extra Factoring Practice (2) Feb 12

11.) $3m^2 - 19m - 20$ $ac = 3 \times -20 = -60 \rightarrow 3 \times (-20)$
 $b = -19$
 ~~$\frac{4}{\cancel{4}} \times \frac{15}{\cancel{15}}$~~
= Not factorable

12) $6x^2 - 27x - 15$

$$\begin{aligned}
 &= 3(2x^2 - 9x - 5) & ac = 2 \times -5 = -10 & b = -9 \\
 &= 3(2x^2 - 10x + x - 5) & (-10) \times 1 \\
 &= 3(2x(x-5) + (x-5)) \\
 &= 3((x-5)(2x+1)) \\
 &= 3(x-5)(2x+1)
 \end{aligned}$$

13) $6x^2 + 17xy + 5y^2$ $ac = 6 \times 5y^2 = 30y^2 \rightarrow 15y \times 2y$
 $b = 17y$

$$\begin{aligned}
 &= 6x^2 + 15xy + 2xy + 5y^2 \\
 &= 2x(3x+y) + 5y(3x+y) \\
 &= (3x+y)(2x+5y)
 \end{aligned}$$

14) $4x^4 + 35x^2 + 49$ $ac = 4 \times 49 = 196$
 $b = 35$

$$\begin{aligned}
 &= 4x^4 + 28x^2 + 7x^2 + 49 \\
 &= 4x^2(x^2 + 7) + 7(x^2 + 7) \\
 &= (x^2 + 7)(4x^2 + 7)
 \end{aligned}$$

$$15) 8x^2 + 38x + 45$$

$$ac = 8 \times 45 = 360$$

$$b = 38$$

∴ Not factorable

$$16) 42t + t - 56t^2 \quad \cancel{ac=}$$

Not going to be on the test

$$17) 10x^2 - 11x + 3 \quad ac = 10 \times 3 = 30 \rightarrow (-5) \times (-6)$$

$$= 10x^2 - 5x - 6x + 3 \quad b = -11$$

$$= 5x(2x-1) - 3x(2x-1)$$

$$= (5x-3x)(2x-1)$$

$$18) x^2 - 121 \quad a = x$$

$$= x^2 - 11^2 \quad b = 11$$

$$= (x+11)(x-11)$$

$$19) x^2 - 20x + 100 \rightarrow \text{Perfect Square}$$

$$= x^2 - 2(1)(10) + 10^2 \quad a = x$$

$$= (x-10)^2 \quad b = 10$$

$$-2ab = -20x$$

$$20) 81x^2 - 18x + 1 \rightarrow \text{Perfect Square}$$

$$= (9x)^2 - (2 \cdot 9x \cdot 1) + 1^2 \quad a = 9x$$

$$= (9x-1)^2 \quad b = 1$$

Extra factoring (3)

$$21) x^4 - 1 \quad a = x^2 \quad \text{Difference of square}$$
$$= (x^2)^2 - 1^2 \quad b = 1$$

$$= (x^2 + 1)(x^2 - 1)$$
$$= (x^2 + 1)(x + 1)(x - 1)$$

$$22) 7x^2 - 343$$

$$= 7(x^2 - 49)$$
$$= 7(x + 7)(x - 7)$$

$$23) 18x^2 + 12x + 8$$
$$= 2(9x^2 + 6x + 4)$$

\downarrow
Done.

$$ac = 4 \times 9 = 36$$
$$b = 6$$

$$26) x^2 - 3x - 40 \quad ac = 1 \times -40 = -40 \rightarrow -8 \times 5$$
$$b = -3$$
$$= (x - 8)(x + 5)$$

$$27) 2x^2 - 2x - 24$$
$$= 2(x^2 - x - 12) \quad ac = -12 \rightarrow (-4) \times 3$$
$$b = -1$$
$$= 2(x - 4)(x + 3)$$

