

What do you have to study for this unit test?

1. Class notes and class work we did from March 23 until today. (Check reypark.weebly.com, if you lost any notes....)
2. All the homework questions we did from March 23 until today.
3. Today's classwork and HW

Note: Leave radical numbers as their original forms, meaning do not change them to decimal numbers until the therefore statement.

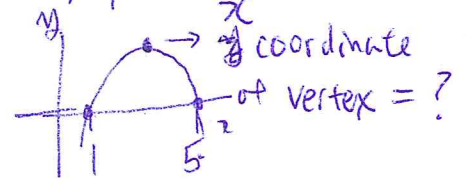
Q1) Last year, a banquet hall charged \$40 per person, and 80 people attended the banquet dinner. This year, the manager said that for every 10 extra people that attended the banquet, they will decrease the price by \$1.50 per person. What size group would maximize the revenue for the hall this year?

Let x represent the increase of people by ~~10~~ ^{more} 10 people. For example
 when $x=1 \rightarrow 10^{\text{more}}$ people will attend. \rightarrow price \downarrow by \$1.50.

Let $F(x)$ (y) represent revenue.

$F(x) = \text{Rev} = \text{Price} \times \text{Quantity}$ (= how many you sold)

$$F(x) = (40 - 1.5x) \times (80 + 10x)$$



$$0 = (40 - 1.5x)(80 + 10x)$$

$$* \text{ If } 40 - 1.5x = 0 \rightarrow y = 0$$

$$-1.5x = -40$$

$$x = (-40) \div (-1.5) = \frac{-40}{-1.5} = 26.67$$

$$* \text{ If } 80 + 10x = 0 \rightarrow y = 0$$

$$10x = -80$$

$$x = -8$$

Answer

$$80 + 10(9.3) = 173 \text{ people}$$

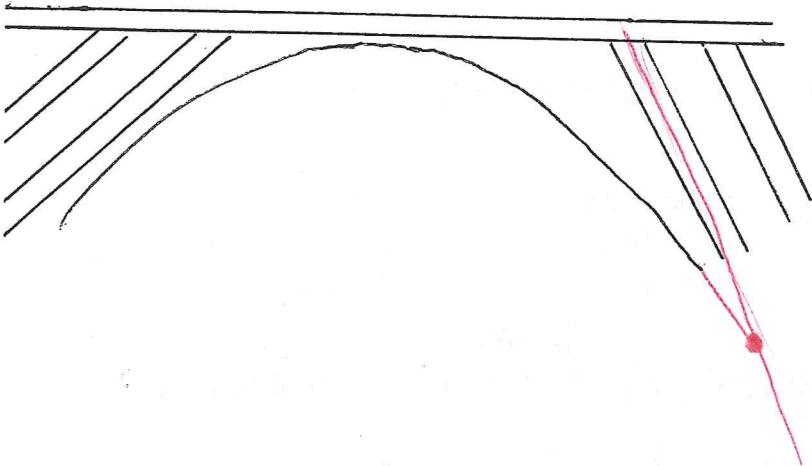
\therefore 173 people would maximize the revenue for this year.

$$* \text{ To find } x \text{ coordinate of vertex: } \frac{-8 + 26.67}{2} = 9.3$$

$$* \text{ sub } x=9.3 \text{ into equation } F(x) = (40 - 1.5(9.3)) \times (80 + 10(9.3)) = 26.05 \times 173 = \$4506.65$$

Q2) A bridge has a parabolic support modelled by the equation $y = -\frac{1}{200}x^2 + \frac{6}{25}x - 5$

Were the x axis represents the bridge surface. There are also parallel support beams below the bridge. Each support beam must have a slope of either 0.8 or -0.8. Using a slope of -0.8, find the y intercept of the line associated with the longest support beam. Hint: The longest beam will be the one along the line that touches the parabolic support at just one point. $b^2 - 4ac = 0$



$y = -0.8x + b$
 $-0.8x + b = -\frac{1}{200}x^2 + \frac{6}{25}x - 5$

$0 = -\frac{1}{200}x^2 + \frac{6}{25}x + \frac{8}{10}x - 5 - b$

$0 = -\frac{1}{200}x^2 + \frac{12x + 40x}{50} - 5 - b$

$0 = -\frac{1}{200}x^2 + \frac{52x}{50} - 5 - b$

$0 = x^2 - 208x + 1000 + 200b$

$* b^2 - 4ac = 0$

$(-208)^2 - 4(1)(1000 + 200b) = 0$

$43264 - 4(1000 + 200b) = 0$

$43264 - 4000 - 800b = 0$

$39264 - 800b = 0$

$\frac{-800b}{-800} = \frac{-39264}{-800}$

$b = 49.08$

\therefore The y intercept is 49.08 of the tangent line