

April 22

Appreciation and Depreciation

* Unit test will be Monday, April 27

Recall: Calculate the total cost, with tax, of a book that is priced at \$29.99.

$$\$29.99 (0.13) + \$29.99 = 3.90 + \$29.99 = 33.89$$

$$\$29.99 \times 1.13 = 33.89 \rightarrow \text{We use this method in this unit.}$$

Was your calculation one step? If not, figure out how to calculate the total cost in one step.

Example 1 Compound Interest

// 0.06

In 2000, \$1000 was invested at a rate of 6% per year for 4 years.

$$\$1000 = A$$

a) How much money was there after 4 years?

$$1.06 = B$$

Number of years	Money
0	\$ 1000
1	\$ 1000 (1.06) = \$ 1060
2	\$ 1060 (1.06) = \$ 1123.60
3	\$ 1123.60 (1.06) = \$ 1191.02
4	\$ 1191.02 (1.06) = \$ 1262.48

b) Write an equation to model this growth.

$$y = 1000 (1.06)^x$$

Let x be # of years
Let y be amount of money

b) How much money is there after 25 years?

When $x = 25$ years, $y = ?$

$$y = 1000 (1.06)^{25}$$

$$y = \$4291.87$$

Example 2 Population Growth

The world population has just reached 7 billion people and the average growth rate is about 1.1%/a.

$$1.1\% = \frac{1.1}{100} = 0.011 \Rightarrow b = 1 + 0.011 = 1.011$$

a) Assuming the growth rate stays the same, what will the population be in 5 years?

Number of years	Number of people
0	7,000,000,000 = a
1	7,000,000,000 (1.011) = 7,077,000,000
2	7,077,000,000 (1.011) = 7,154,847,000
3	7233550317
4	7313119370
5	7393563684

b) Write an equation to model this growth.

$$Y = 7000,000,000 (1.011)^x$$

Let Y be population

Let x be # of years.

Example 3 Depreciation

A new car costs \$24 000. It loses 18% of its value each year after it is purchased.

a) Determine the equation that models the value of the car.

Age of Car	Value of Car
0	\$ 24000
1	\$24000 × 0.82 = \$19680
2	\$19680 × 0.82 = \$16137.60

Let Y be the car's value

Let x be the # of years

$$Y = 24000 (0.82)^x$$

$$= 1 - 0.18 = 0.82$$

= b

$$100\% - 18\% = 82\%$$

* After first year, you have calculate:

$$\begin{aligned} \$24000 - 0.18(\$24000) \\ = \$19680 \end{aligned}$$

b) Use your equation to determine the value of the car after 30 months.

$$\frac{30 \text{ months}}{12 \text{ months}} = 2.5 \text{ years} \quad y = 24000 (0.82)^{2.5}$$

$$= \$ 14613.22$$

c) Determine the number of years it will take for the car to depreciate to one-half of its original value.

$$24000 \div 2 = 12000 \rightarrow \text{When } y = 12000, x = ?$$

$$\frac{12000}{24000} = \frac{24000 (0.82)^x}{24000}$$

$$\frac{1}{2} = 0.82^x$$

You have to guess and check until you find the answer

$$0.5 = 0.82^{3.49}$$

$$\therefore x = 3.49$$

\therefore It takes 3.49 years to depreciate to one-half of its original value.

* Grade 12 Method: $\rightarrow \log 0.5 = \log 0.82^x \rightarrow \frac{\log 0.5}{\log 0.82} = \frac{x \cdot \log 0.82}{\log 0.82}$

$$x = \frac{\log 0.5}{\log 0.82} = 3.49$$

Example 4 Determine equations for the following:

a) A town with a population of 12 000 has been growing at an average rate of 2.5% for the last 10 years. Suppose this growth rate will be maintained in the future.

$$y = 12000 (1.025)^x$$

Let y be population
Let x be # of years

$$\Rightarrow b = 1 + 0.025 = 1.025$$

b) Find an equation for the situation above but for population in the thousands.

$$y = 12 (1.025)^x$$

same "Let statements" as above.